# **Photomtery Systems**

- Introduction
  - flux
  - magnitudes
    - Pogson, AB, ST, asinh
- Systems
  - ADPS database
  - conversions

- SDSS
  - ugriz system
  - which magnitude to use ?

### M. G. Allen, October 26, 2006 – material from:

George Djorgovski's lecture notes: http://www.astro.caltech.edu/~george/ay122/Ay122-photometry.pdf
Asiago Database of Photometric Systems: http://ulisse.pd.astro.it/Astro/ADPS/
Sloan Digitial Sky survey Data Release: http://www.sdss.org/dr5

## **Measuring Flux** = Energy/(unit time)/(unit area)

Real detectors are sensitive over a finite range of  $\lambda$  (or  $\nu$ ). Fluxes are always measured over some finite bandpass.

Total energy flux:  $F = \int_{-\infty}^{\infty} F_{v}(v) dv$  Integral of  $f_{v}$  over all frequencies

Units: erg s<sup>-1</sup> cm<sup>-2</sup> Hz<sup>-1</sup>

A standard unit for specific flux (initially in radio, but now more common):

1 Jansky (Jy) =  $10^{-23}$  erg s<sup>-1</sup> cm<sup>-2</sup> Hz<sup>-1</sup>

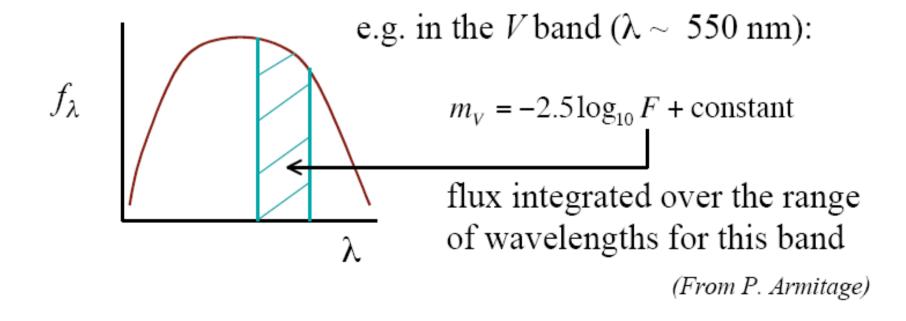
 $f_{v}$  is often called the *flux density* - to get the *power*, one integrates it over the bandwith, and multiplies by the area

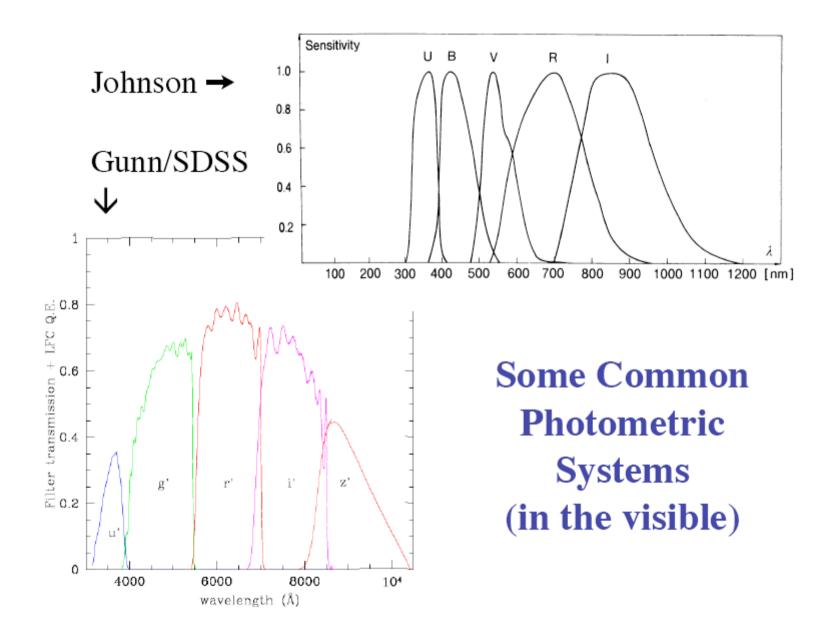
(From P. Armitage)

## Fluxes and Magnitudes

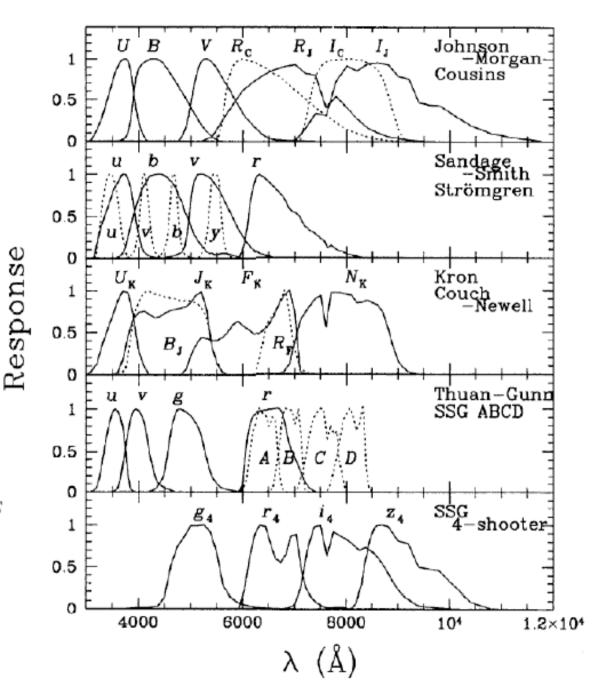
For historical reasons, fluxes in the optical and IR are measured in magnitudes:  $m = -2.5 \log_{10} F + \text{constant}$ 

If F is the total flux, then m is the bolometric magnitude. Usually instead consider a finite bandpass, e.g., V band.



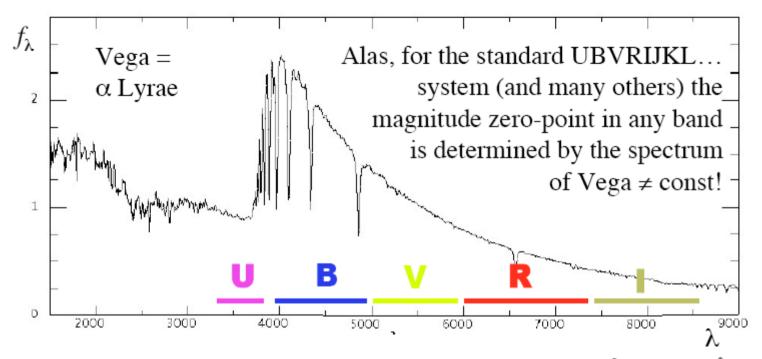


There are way, way too many photometric systems out there ...



(Bandpass curves from Fukugita et al. 1995, PASP, 107, 945)

## **Magnitude Zero Points**



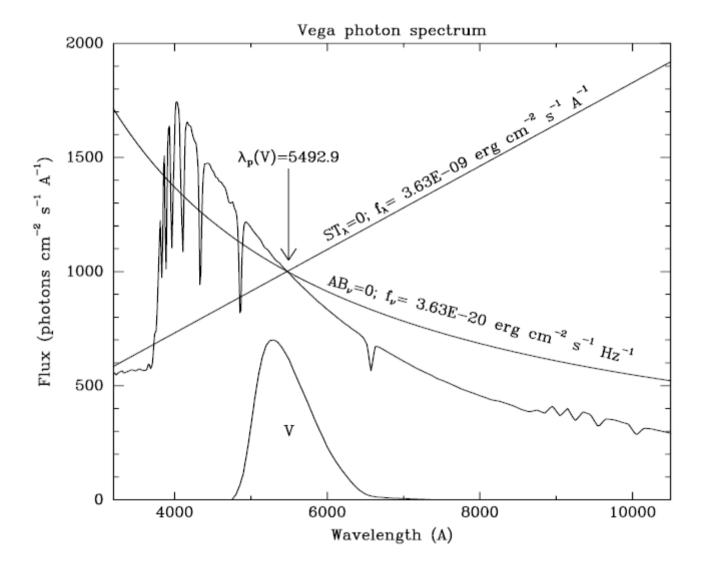
Vega calibration (m = 0): at  $\lambda = 5556$ :  $f_{\lambda} = 3.39 \times 10^{-9} \text{ erg/cm}^2/\text{s/Å}$ 

 $f_{\lambda} = 3.39 \times 10^{-9} \text{ erg/cm}^2/\text{s/A}$  $f_{\nu} = 3.50 \times 10^{-20} \text{ erg/cm}^2/\text{s/Hz}$ 

 $N_{\lambda} = 948 \text{ photons/cm}^2/\text{s/Å}$ 

A more logical system is  $AB_v$  magnitudes:

 $AB_{\rm v} = -2.5 \log f_{\rm v} \,[{\rm cgs}] - 48.60$ 



# Magnitude definitions

- Pogson:  $m = -2.5 \log_{10}(F) + constant$
- Vega:  $m = -2.5 \log_{10}(F/F_{vega})$

$$m_i = -2.5 \log_{10} \frac{\int R_i(\lambda) F_\lambda(\lambda) d\lambda}{\int R_i(\lambda) F_\lambda^{\mathrm{VEGA}}(\lambda) d\lambda} + 0.03$$

Inverse hyperbolic sine magnitudes

$$m = [-2.5 / ln(10)] * [asinh((F/F0)/2b) + ln(2b)]$$

# **Monochromatic Magnitudes**

$$m_{\lambda}(\lambda) \equiv -2.5 \log_{10} F_{\lambda}(\lambda) - 21.1$$

where  $F_{\lambda}(\lambda)$  is the <u>spectral flux density</u> of a source at the top of the Earth's atmosphere in units of erg s<sup>-1</sup> cm<sup>-2</sup> Å<sup>-1</sup>. This is also known as the "STMAG" system because it is standard for the Hubble Space Telescope.

The corresponding system based on flux per unit frequency is

$$m_{\nu}(\lambda) \equiv -2.5 \log_{10} F_{\nu}(\lambda) - 48.6$$

where  $F_{\nu}(\lambda)$  is in units of erg s<sup>-1</sup> cm<sup>-2</sup> Hz<sup>-1</sup>. This is also known as the "AB" or "AB<sub> $\nu$ </sub>" system.

## Conversions among magnitude systems:

#### Conversion from AB magnitudes to Johnson magnitudes:

The following formulae convert between the AB magnitude systems and those based on Alpha Lyra:

```
V = V(AB) + 0.044 (+/- 0.004)
B = B(AB) + 0.163 (+/- 0.004)
Bj = Bj(AB) + 0.139 (+/- INDEF)
R = R(AB) - 0.055 (+/- INDEF)
I = I(AB) - 0.309 (+/- INDEF)
g = g(AB) + 0.013 (+/- 0.002)
r = r(AB) + 0.226 (+/- 0.003)
i = i(AB) + 0.226 (+/- 0.005)
u' = u'(AB) + 0.0
g' = g'(AB) + 0.0
g' = g'(AB) + 0.0
r' = r'(AB) - 0.0
c' = z'(AB) - 0.117 (+/- 0.006)
IC = IC(AB) - 0.342 (+/- 0.008)
```

Source: Frei & Gunn 1995



### the Asiago Database on Photometric Systems

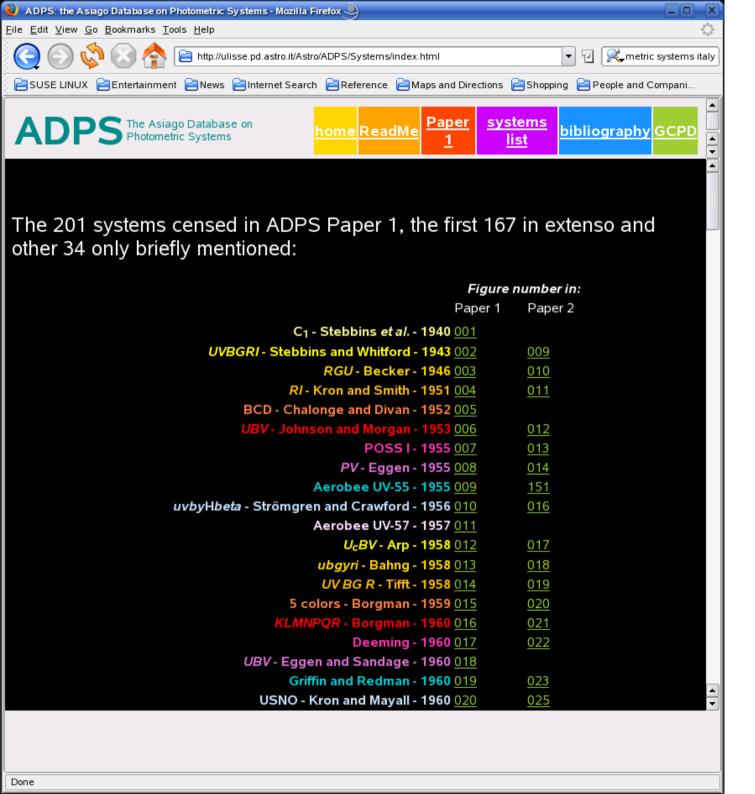
by Ulisse Munari, Massimo Fiorucci and Dina Moro

The Asiago Database on Photometric Systems (<u>ADPS</u>) project aims to cense and investigate existing photometric systems.

<u>Paper 1</u> (Moro and Munari 2000, A&AS 147, 361) presents a compilation of basic information and reference data from literature for 201 photometric systems (167 censed in extenso, and 34 only briefly noted). General ascii lists about systems and bands can be found <u>here</u>.

Paper 2 (Fiorucci and Munari 2002, A&A, submitted) adds further 17 systems, bringing the total to 218 censed systems, and provides homogeneous band and reddening parameters for all the systems with known band transmission profiles (179). Spectra and reddening curves used in the synthetic photometry computation can be found here.

Planned Paper 3 will deal with calibration of the systems in terms of basic physical stellar parameters (temperature, gravity, metallicity, reddening), and Paper 4 with transformations between the systems.



## ADPS 2 The Asiago Database on Photometric Systems

#### Sloan DSS - Fukugita et al. - 1996 u ´ r´ z´ gĺ 2600 3 800 5000 6200 7400 8600 9800 11000 λ(Å) $\mathbf{u}'$ B3SunK2M2CarbonVega $\lambda_c = 3530$ $\lambda_0 = 3521$ $\lambda_{peak} = 3431$ 3504 3538 3593 3636 3525 $\lambda_{gauss} = 3519$ 3551WHM = 642W10% = 831W80% = 437FWHM = 555[599] [602] [565][517][448][498] $\frac{A(\lambda)}{A(V)}|_{5.0} = 1.36^{+1.34}_{-1.40}$ $a = {0.934 \atop 0.944} b = {2.036 \atop 1.972}$ $PN^{Ne}$ $PN_{Ne}$ $W_0 = 590$ WNWCNovaWDA $a = {0.942 \atop 0.949} b = {1.985 \atop 1.934}$ $|_{3.1} = 1.61^{+1.58}_{-1.69}$ $\mu = 201$ 3489 3500 3642 3533 3481 3517 $\frac{A(\lambda)}{E(B-V)}$ : $(4.946, 0.067)_{B3}^{r=0.99}$ $\frac{A(\lambda)}{A(V)}|_{2.1} = 1.95^{+0.88}_{-0.08}$ $(5.271, 0.091)_{Sun}^{r=1.00}$ $(5.888, 0.075)_{M2}^{r=1.00}$ $I_{asym} = 0.01$ $W_{eff} = 600.1 - 38.8 \times E(B - V)$ r=-0.98 $\lambda_{eff} = 3521.5 + 41.9 \times E(B - V)$ r=1.00 $I_{kurt} = -0.88$ $\lambda_{eff}(T) = 3472 + 145 \times \theta + 77 \times \theta^2 - 55 \times \theta^3$ $W_{eff}(T) = 556 + 263 \times \theta - 562 \times \theta^2 + 193 \times \theta^3$ $\mathbf{g}'$ B3SunK2VegaM2Carbon $\lambda_c = 4788$ 4683 4817 4903 5100 $\lambda_0 = 4803$ $\lambda_{peak} = 5173$ $\lambda_{gauss} = 4820$ 4708 5015 WHM = 1411W10% = 1641W80% = 1111 FWHM = 1245 [1238][1271] [1318] [1230] [1057] [1004] $\frac{A(\lambda)}{A(V)}|_{5.0} = 1.12^{+1.10}_{-1.13}$ $a = {}^{1.011}_{1.015} b = {}^{0.656}_{0.486}$ WN $PN^{Ne}$ $W_0 = 1325$ WC $PN_{Ne}$ NovaWDA $a = {}^{1.015}_{1.016} b = {}^{0.507}_{0.371} Sun$ $|_{3.1} = 1.19 \stackrel{1.16}{}_{1.20}$ 4767 $\mu = 419$ 4696 4706 4943 49234716 $\frac{A(\lambda)}{E(B-V)}$ : $(3.804, -0.006)_{B3}^{r=-0.78}$ $(4.281, -0.000)_{M2}^{r=-0.08}$ $|_{2.1} = 1.28 \stackrel{1.24}{_{1.30}}$ $(3.949, 0.009)_{Sun}^{r=0.95}$ $I_{asym} = -0.12$ $\lambda_{eff} = 4807.4 + 142.3 \times E(B - V)$ r=1.00 $I_{kurt} = -1.04$ $W_{eff} = 1371.8 - 208.0 \times E(B - V)$ r=-0.99 $\lambda_{eff}(T) = 4647 + 312 \times \theta + 241 \times \theta^2 - 173 \times \theta^3$ $W_{eff}(T) = 1156 + 909 \times \theta - 1424 \times \theta^2 + 387 \times \theta^3$ $\mathbf{r}'$ B3VegaSun $K_2^o$ M2Carbon $\lambda_c = 6242$ $\lambda_{\circ} = 6253$ 6220 6256 6307 6365 $\lambda_{peak} = 6191$ $\lambda_{gauss} = 6247$ 6160 6168 WHM = 1387W10% = 1565W80% = 1248 FWHM = 1262 [1335][1282] [1294] [1341][1315][1251] $\frac{A(\lambda)}{A(V)}|_{5.0} = 0.88^{0.88}_{0.89}$ $a = {0.947 \atop 0.938} b = {-0.205 \atop -0.224}$ $PN^{Ne}$ $PN_{Ne}$ $W_{\circ} = 1343$ WNWCNovaWDA $|_{3.1} = 0.83^{+0.84}_{-0.85}$ $a = {0.941 \atop 0.933} b = {-0.218 \atop -0.235}$ $\mu = 407$ 6220 6432 6124653164446156 $\frac{A(\lambda)}{E(B-V)}$ : $(2.615, 0.020)_{B3}^{r=0.99}$ $\frac{A(\lambda)}{A(V)}|_{2.1} = 0.77^{+0.77}_{-0.79}$ $(2.770, 0.028)_{Sun}^{r=1.00}$ $(3.099, 0.013)_{M2}^{r=0.98}$ $I_{asym} = -0.01$ $\lambda_{eff} = 6253.4 + 91.0 \times E(B - V)$ r=1.00 $I_{kurt} = -1.09$ $W_{eff} = 1370.2 - 106.1 \times E(B - V)$ r=-0.98 $\lambda_{eff}(T) = 6145 + 139 \times \theta + 156 \times \theta^2 - 80 \times \theta^3$ $W_{eff}(T) = 1255 + 289 \times \theta - 183 \times \theta^2 - 109 \times \theta^3$

TABLE 9
Characteristics of Photometric Bands

bandpass system	band	$ref^{a)}$	$\lambda_{ ext{eff}}$	FWHM	$\lambda_{ ext{eff}}^{ ext{Vega}}$	$f_{\lambda_{i}^{-}  ext{eff}}^{ ext{Vega}}$	$c( u_{ m eff}^{ m Vega})^{-1}$	$f_{ u, ext{eff}}^{ ext{Vega}}$
			(Å)	(Å)	(Å)	$(\times 10^{-9} \text{cgs/Å})$	(Å)	$(\times 10^{-20} \text{cgs/Hz})$
Johnson-Morgan	$U_3$	Buser 78	3652	526	3709	4.28	3617	1.89
	$B_2$	AS69	4448	1008	4393	6.19	4363	4.02
	V	AS69	5505	827	5439	3.60	5437	3.59
Cousins	$R_{\mathrm{C}}$	Bessell 90	6588	1568	6410	2.15	6415	3.02
	$I_{ m C}$	Bessell 90	8060	1542	7977	1.11	7980	2.38
Johnson	$R_{ m J}$		6930	2096	6688	1.87	6693	2.89
	$I_{ m J}$		8785	1706	8571	0.912	8545	2.28
Sandage-Smith	u		3647	595	3710	4.30	3610	1.89
	b		4466	1028	4407	6.10	4369	3.97
	v		5423	823	5368	3.75	5365	3.64
	r		6712	969	6628	1.96	6629	2.90
Strömgren	u	Olson74	3465	363	3496	3.24	3452	1.31
	$\boldsymbol{v}$	Matsu69	4109	197	4119	7.21	4103	4.12
	b	Olson74	4668	176	4666	5.68	4663	4.15
	$\boldsymbol{y}$	Olson74	5459	244	5455	3.62	5453	3.60
Kron	$U_{\mathbf{K}}$	Koo 85	3656	556	3737	4.32	3617	1.93
	$J_{ m K}$		4625	1550	4537	5.54	4467	3.82
	$F_{ m K}$		6168	1330	5978	2.64	5982	3.25
	$N_{ m K}$		7953	1786	7838	1.17	7842	2.44
Couch-Newell	$B_{ m J}$		4604	1490	4515	5.73	4474	3.95
	$R_{ m F}$		6694	517	6679	1.92	6677	2.86

5

### Empirical Color Transformations Between SDSS Photometry and Other Photometric Systems

K. Jordi\*, E.K. Grebel, and K. Ammon

Astronomical Institute of the University of Basel, Department of Physics and Astronomy, Venusstrasse 7, CH-4102 Binningen, Switzerland —e-mail: jordi@astro.unibas.ch, grebel@astro.unibas.ch, ammon@astro.unibas.ch

Received August 14, 2006; accepted August 28, 2006

#### ABSTRACT

Aims. We present empirical color transformations between the Sloan Digital Sky Survey (SDSS) ugriz photometry and Johnson-Cousins UBVRI system and Becker's RGU system, respectively. Owing to the magnitude of data that is becoming available in the SDSS photometric system it is particularly important to be able to convert between this new system and traditional photometric systems. Unlike earlier published transformations we based our calculations on stars actually measured by the SDSS with the SDSS 2.5-m telescope. The photometric database of the SDSS provides in a sense a single-epoch set of 'tertiary standards' covering more than one quarter of the sky. Our transformations should facilitate their use to easily and reliably derive the corresponding approximate Johnson-Cousins or RGU magnitudes.

Methods. The SDSS survey covers a number of areas that were previously established as standard fields in the Johnson-Cousins system, in particular, fields established by Landolt and by Stetson. We used these overlapping fields to create well-photometered star samples on which our calculated transformations are based. For the RGU photometry we used fields observed in the framework of the new Basel high-latitude field star survey.

Results. We calculated *empirical* color transformations between SDSS photometry and Johnson-Cousins *UBVRI* and Becker's *RGU* system. For all transformations we found linear relations to be sufficient. Furthermore we showed that the transformations between the Johnson-Cousins and the SDSS system have a slight dependence on metallicity.

#### 3. Results

### 3.1. Transformations between SDSS and Johnson–Cousins Photometry

The transformation between the Johnson–Cousins *UBVRI* photometry system and the SDSS *ugriz* system was carried out using the following eight general equations:

$$g-V = a_1 (B-V) + b_1$$
  
 $r-i = a_2 (R-I) + b_2$   
 $r-z = a_3 (R-I) + b_3$   
 $r-R = a_4 (V-R) + b_4$   
 $u-g = a_5 (U-B) + b_5 (B-V) + c_5$   
 $g-B = a_6 (B-V) + b_6$   
 $g-r = a_7 (V-R) + b_7$   
 $i-I = a_8 (R-I) + b_8$ 

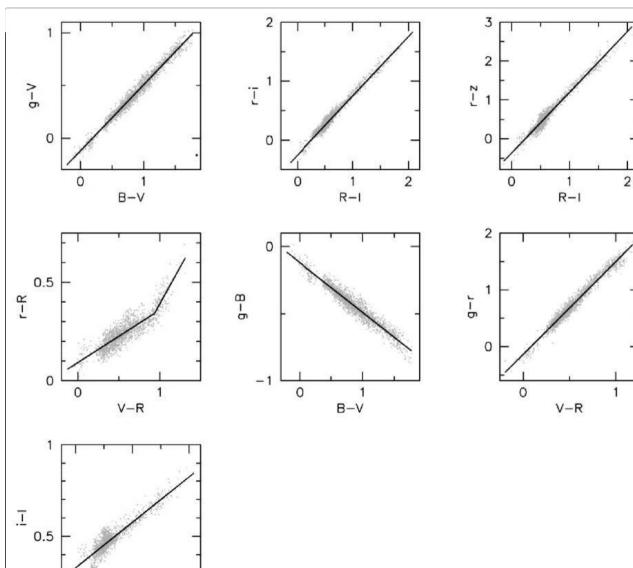


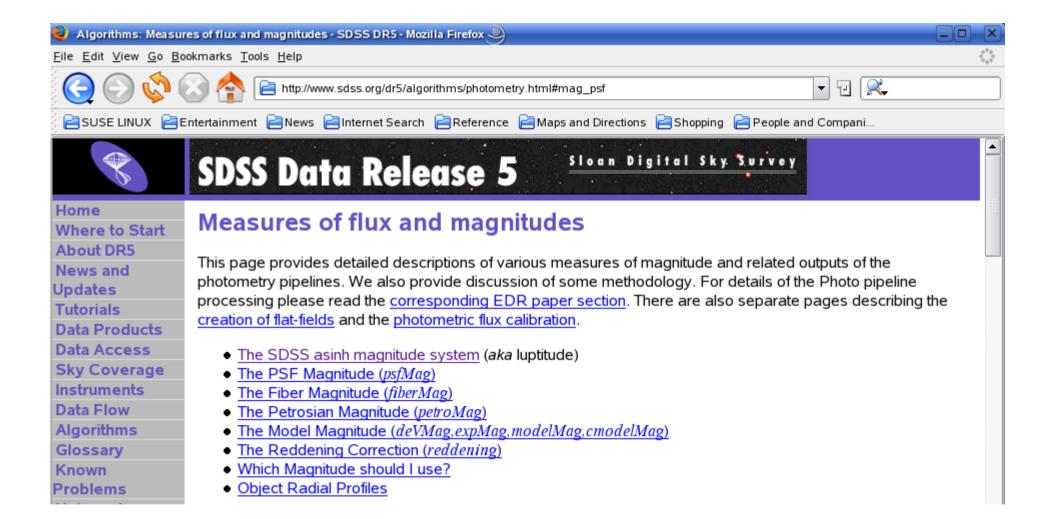
Table 3. Coefficients of the 'global' transformations between UBVRI and ugriz (equations 1–8)

Color	Color Term	Zeropoint	Range
g-V	$(0.630 \pm 0.002) (B - V)$	$-(0.124 \pm 0.002)$	
r-i	$(1.007 \pm 0.005) (R - I)$	$-(0.236 \pm 0.003)$	
r-z	$(1.584 \pm 0.008) (R - I)$	$-(0.386 \pm 0.005)$	
r-R	$(0.267 \pm 0.005) (V - R)$	$+(0.088 \pm 0.003)$	$V - R \le 0.93$
r-R	$(0.77 \pm 0.04) (V - R)$	$-(0.37 \pm 0.04)$	V - R > 0.93
u-g	$(0.750 \pm 0.050) (U - B) + (0.770 \pm 0.070) (B - V)$	$+(0.720 \pm 0.040)$	
g - B	$-(0.370 \pm 0.002) (B-V)$	$-(0.124 \pm 0.002)$	
g-r	$(1.646 \pm 0.008) (V - R)$	$-(0.139 \pm 0.004)$	
i-I	$(0.247 \pm 0.003) (R - I)$	$+(0.329 \pm 0.002)$	

$$g = V + (0.630 \pm 0.002)(B - V) - (0.124 \pm 0.002)$$

 $\textbf{Table 4.} \ \ \textbf{Metallicity-dependent transformations between} \ \ \textit{BVRI} \ \ \textbf{and} \ \ \textit{griz} \ \ \textbf{for metal-poor Population II} \ \ \textbf{and more metal-rich Population I stars}.$ 

Color	Color Term	Zeropoint	Validity
g – V	$(0.634 \pm 0.002) (B - V)$	$-(0.127 \pm 0.002)$	Population I
g-V	$(0.596 \pm 0.009) (B - V)$	$-(0.148 \pm 0.007)$	metal-poor Population II
r - i	$(0.988 \pm 0.006) (R - I)$	$-(0.221 \pm 0.004)$	Population I
r - i	$(1.06 \pm 0.02) (R - I)$	$-(0.30 \pm 0.01)$	metal-poor Population II
r-z	$(1.568 \pm 0.009) (R - I)$	$-(0.370 \pm 0.006)$	Population I
r-z	$(1.60 \pm 0.06) (R - I)$	$-(0.46 \pm 0.03)$	metal-poor Population II
r-R	$(0.275 \pm 0.006) (V - R)$	$+(0.086 \pm 0.004)$	$V - R \le 0.93$ ; Population I
r-R	$(0.71 \pm 0.05) (V - R)$	$-(0.31 \pm 0.05)$	V - R > 0.93; Population I
r-R	$(0.34 \pm 0.02) (V - R)$	$+(0.015 \pm 0.008)$	$V - R \le 0.93$ ; metal-poor Population II
g - B	$-(0.366 \pm 0.002) (B-V)$	$-(0.126 \pm 0.002)$	Population I
g - B	$-(0.401 \pm 0.009) (B-V)$	$-(0.145 \pm 0.006)$	metal-poor Population II
g-r	$(1.599 \pm 0.009) (V - R)$	$-(0.106 \pm 0.006)$	Population I
g-r	$(1.72 \pm 0.02) (V - R)$	$-(0.198 \pm 0.007)$	metal-poor Population II
i-I	$(0.251 \pm 0.003) (R - I)$	$+(0.325 \pm 0.002)$	Population I
i-I	$(0.21 \pm 0.02) (R - I)$	$+(0.34 \pm 0.01)$	metal-poor Population II



# SDSS magnitudes:

AB system, asinh magnitudes

- Fiber Magnitudes flux in fiber aperture
- Model Magnitudes
  - model fits to objects using deVaucoulers profile, expoinential profile – relevant to galaxies
- Cmodel Magnitudes
  - flux in linear combination of best fitting models
- Petrosian Magnitudes
  - flux in circular aperture with r defined by azimuthally averaged light profile RP<sub>P,lim</sub> ~0.2
- PSF magnitudes
  - Point Spread Function fit for isolated stars

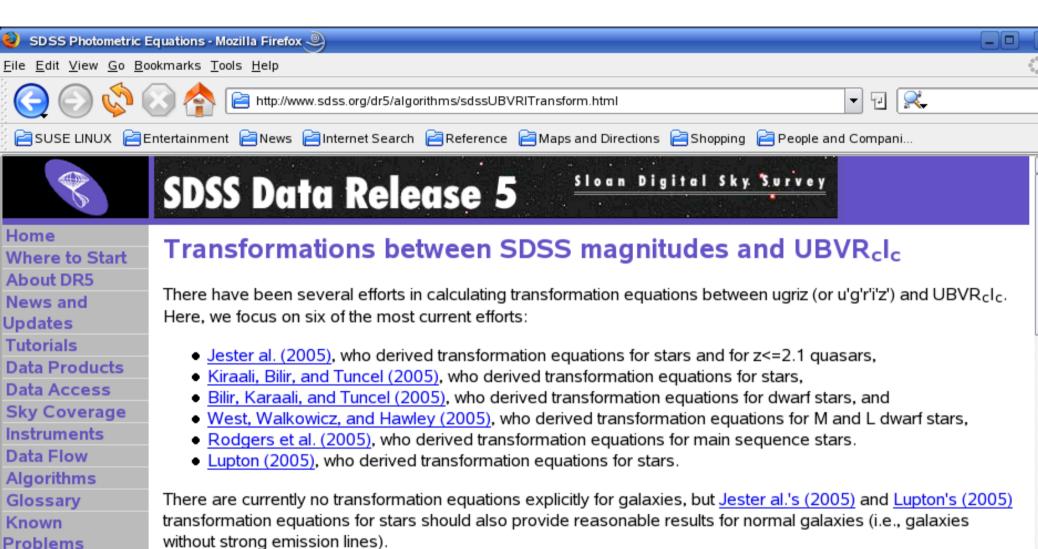
### Which Magnitude should I use?

Faced with this array of different magnitude measurements to choose from, which one is appropriate in which circumstances? We cannot give any guarantees of what is appropriate for the science *you* want to do, but here we present some examples, where we use the general guideline that one usually wants to maximize some combination of signal-to-noise ratio, fraction of the total flux included, and freedom from systematic variations with observing conditions and distance.

Given the excellent agreement between *cmodel* magnitudes (see <u>cmodel magnitudes</u> above) and PSF magnitudes for point sources, and between *cmodel* magnitudes and Petrosian magnitudes (albeit with intrinsic offsets due to aperture corrections) for galaxies, the *cmodel* magnitude is now an adequate proxy to use as a universal magnitude for all types of objects. As it is approximately a matched aperture to a galaxy, it has the great advantage over Petrosian magnitudes, in particular, of having close to optimal noise properties.

#### Example magnitude usage

- **Photometry of Bright Stars**: If the objects are bright enough, add up all the flux from the profile *profMean* and generate a large aperture magnitude. We recommend using the first 7 annuli.
- Photometry of Distant Quasars: These will be unresolved, and therefore have images consistent with the PSF. For this reason, psfMag is unbiased and optimal.
- Colors of Stars: Again, these objects are unresolved, and psfMag is the optimal measure of their brightness.
- Photometry of Nearby Galaxies: Galaxies bright enough to be included in our spectroscopic sample
  have relatively high signal-to-noise ratio measurements of their Petrosian magnitudes. Since these
  magnitudes are model-independent and yield a large fraction of the total flux, roughly constant with redshift,
  petroMag is the measurement of choice for such objects. In fact, the noise properties of Petrosian
  magnitudes remain good to r=20 or so.
- Photometry of Galaxies: Under most conditions, the cmodel magnitude is now a reliable estimate of the galaxy flux. In addition, this magnitude account for the effects of local seeing and thus are less dependent on local seeing variations.
- Colors of Galaxies: For measuring colors of extended objects, we continue to recommend using the
  model (not the cmodel) magnitudes; the colors of galaxies were almost completely unaffected by the DR1
  software error. The model magnitude is calculated using the best-fit parameters in the r band, and applies it
  to all other bands; the light is therefore measured consistently through the same aperture in all bands.



Help and

Feedback

Search

without strong emission lines).

Caveat: Note that these transformation equations are for the SDSS ugriz (u'g'r'i'z') magnitudes as measured, not for SDSS ugriz (u'g'r'i'z') corrected for AB offsets. If you need AB ugriz magnitudes, please remember to convert from SDSS ugriz to AB ugriz using AB offsets described at this URL).

#### UBVRcIc -> ugriz

===========

## Quasars at z <= 2.1 (synthetic)

	Transfor	rmation	RMS residual
u-g	=	1.25*(U-B) + 1.02	0.03
g-r	=	0.93*(B-V) - 0.06	0.09
r-i	=	0.90*(Rc-Ic) - 0.20	0.07
r-z	=	1.20*(Rc-Ic) - 0.20	0.18
g	=	V + 0.74*(B-V) - 0.07	0.02
r	=	V - 0.19*(B-V) - 0.02	0.08

#### Stars with Rc-Ic < 1.15 and U-B < 0

	Transfor	rmation			RMS residual
u-g	=	1.28*(U-B)	+	1.14	0.05
g-r	=	1.09*(B-V)	-	0.23	0.04
r-i	=	0.98*(Rc-Ic)	-	0.22	0.01
r-z	=	1.69*(Rc-Ic)	-	0.42	0.03
g	=	V + 0.64*(B-V	7)	- 0.13	0.01
r	=	V = 0.46 * (B-V)	7)	+ 0.11	0.03

#### All stars with Rc-Ic < 1.15

	Transfo		RMS residual	
u-g	=	1.28*(U-B) +	1.13	0.06
g-r	=	1.02*(B-V) -	0.22	0.04
r-i	=	0.91*(Rc-Ic) -	0.20	0.03
r-z	=	1.72*(Rc-Ic) -	0.41	0.03
g	=	V + 0.60*(B-V)	- 0.12	0.02
r	=	V - 0.42*(B-V)	+ 0.11	0.03

# What's coming?

- In context of VO
  - Data model for photometry
  - Something like WCS for coordinates, but for photometry to describe photometric systems
  - Problem recognized, but nothing has happended yet...

# Suggestions for SIMBAD

- Convert current B and V mags into SDSS g
  - but current B and V mags have no references (?)
  - choose a published transformation, apply only to stars
- Include SDSS g (or ubgiz) where X-match in SDSS exits
  - and link to SDSS (in Vizier, or SDSS itself)
- Ingest measurements in well specified systems
  - e.g the list from Fukugita et al. 1995
  - contribute to development of Photometry Data Model and serialization

# Magnitudes, A Formal Definition

$$m = -2.5 \left[ \log \int d\lambda R(\lambda) f_{\lambda} - \log \int d\lambda R(\lambda) f_{\lambda}(\alpha \text{ Lyr}) \right]$$

e.g., 
$$U = -2.5 \log \int d\lambda R_U(\lambda) f_{\lambda} - 14.08 + c_U,$$
 
$$B = -2.5 \log \int d\lambda R_B(\lambda) f_{\lambda} - 13.00 + c_B,$$
 
$$V = -2.5 \log \int d\lambda R_V(\lambda) f_{\lambda} - 13.76 + c_V,$$

Because Vega (= α Lyrae) is declared to be the zero-point! (at least for the UBV... system)

where the peak of the response function is normalized to unity, and c represents the magnitude of  $\alpha$  Lyr;  $c_U = 0.02$ ,  $c_B = c_V = 0.03$  (Johnson and Morgan 1953).

Defining effective wavelengths (and the corresponding bandpass averaged fluxes)

$$\lambda_{\text{eff}} = \frac{\int d\lambda \lambda R(\lambda)}{\int d\lambda R(\lambda)},$$

$$f_{\lambda}^{\text{eff}}(\alpha \text{ Lyr}) = \frac{\int d\lambda f_{\lambda}(\alpha \text{ Lyr})R(\lambda)}{\int d\lambda R(\lambda)},$$

$$\lambda_{\text{eff}}(\alpha \text{ Lyr}) = \frac{\int d\lambda \lambda f_{\lambda}(\alpha \text{ Lyr})R(\lambda)}{\int d\lambda f_{\lambda}(\alpha \text{ Lyr})R(\lambda)},$$

$$f_{\nu}^{\text{eff}}(\alpha \text{ Lyr}) = \frac{\int d\nu f_{\nu}(\alpha \text{ Lyr})R(\nu)}{\int d\nu R(\nu)},$$

$$v_{\text{eff}}(\alpha \text{ Lyr}) = \frac{\int d\nu \nu f_{\nu}(\alpha \text{ Lyr}) R(\nu)}{\int d\nu f_{\nu}(\alpha \text{ Lyr}) R(\nu)}$$

where 
$$f_{\nu} = \lambda^2 f_{\lambda}/c$$
 and  $R_{\nu} = R_{\lambda}$ .