

Efficient and scalable cross-matching of (very) large catalogues

François-Xavier Pineau¹, Thomas Boch¹ and Sebastien Derrière¹

¹CDS, Observatoire Astronomique de Strasbourg

ADASS Boston, 08 November 2010



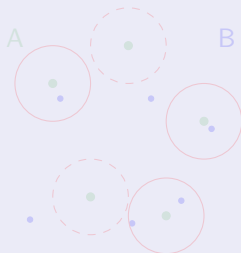
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CDS cross-match service (in development)

- Based on UWS (job submission)
- Catalogues :



- Algorithms :



- Particularity : deal with (very) large catalogues

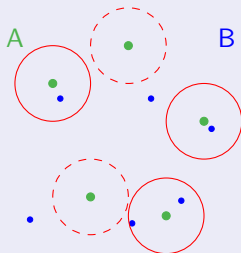
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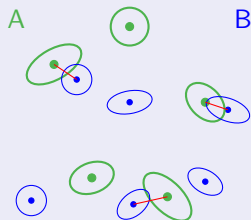
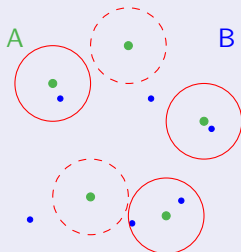
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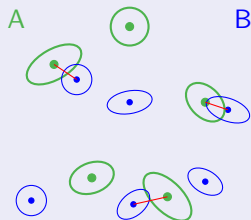
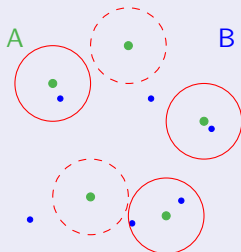
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Dealing with (very) large catalogues

Example

- 2MASS
 - ▶ $\sim 470 \times 10^6$ sources
 - ▶ minimal data ~ 15 GB
 - ★ identifier (integer 4 Bytes)
 - ★ positions (double 8 B+8 B)
 - ★ errors (float 4 B+4 B+4 B)
- USNO-B1
 - ▶ $\sim 10^9$ sources
 - ▶ minimal data ~ 28 GB
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- LSST projection at 5 years:
 - ▶ $V > 26$, $\sim 3 \times 10^9$ **unique** sources
 - ▶ minimal data ~ 96 GB

Problems

- Data size
 - ▶ do not fit into memory
- Performance issues
 - ▶ data loading
 - ▶ looking for candidates

Solutions

- Scalability: Healpix partitioning
- Efficiency:
 - ▶ special indexed binary file
 - ▶ kd-tree (cone search queries)
 - ▶ multithreading
 - ▶ parallel processing

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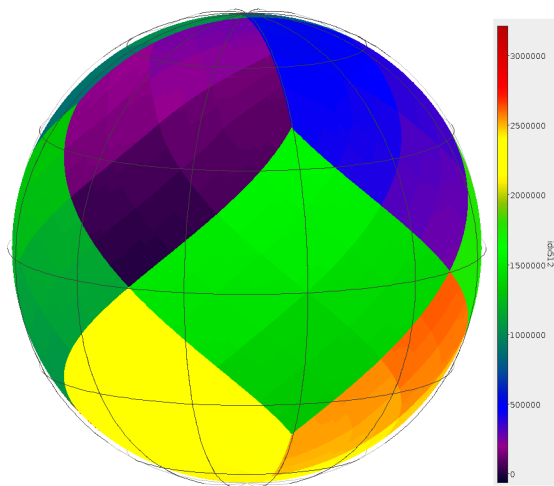
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Healpix

- Hierarchical sky pixelisation
 - ▶ level 0 \rightsquigarrow 12 pixels
 - ▶ level 1 \rightsquigarrow 12x4 pixels
 - ▶ ...
 - ▶ level n \rightsquigarrow 12×2^{2n}
- Pixels of equal area
- Developed at NASA: healpix.jpl.nasa.gov
- Available in
 - ▶ C, C++
 - ▶ Fortran
 - ▶ IDL
 - ▶ Java
 - ▶ ...?



Scalable cross-match

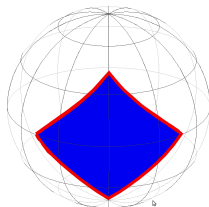
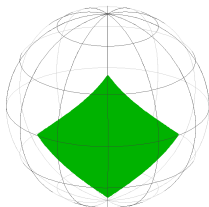
- Independent pixels cross-match
 - ▶ but **border effects**
- Cat. B pixel sources put in a *kd*-tree
- Optimal partitioning level

- ▶ available memory
- ▶ minimisation of:

$$\sum_{i=0}^{nPixels} N_{A_i} \log(1 + N_{B_i} + N_{B_i}^b)$$

- ▶ I/O cost

Level 0



Level 1

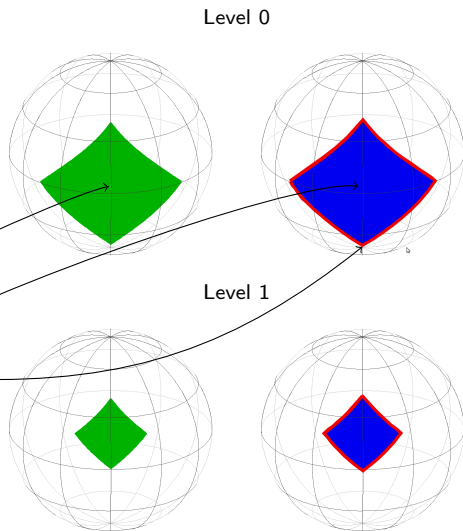
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Scalable cross-match

Single machine

- All sky correlation (small catalogues)
 - ▶ allow “on the fly” correlation
- Correlation pixel by pixel (large catalogues)



Computer grid

- Parallel processing
- Framework:
 - based on UWS^{*} (few machines)
 - Hadoop (large grid)
- “On the fly” correlation possible



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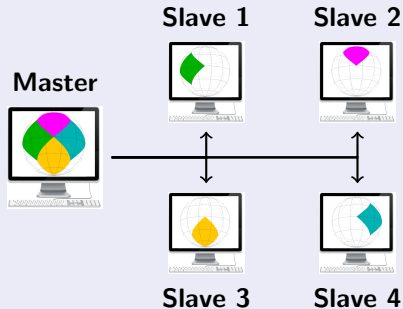
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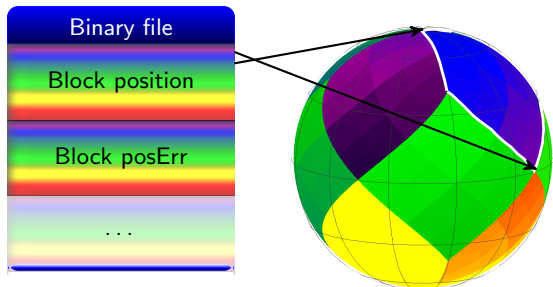
Loading data: indexed binary files

Index files

- One by healpix level
- For each pixel
 - ▶ offset
 - ▶ nSources

Binary data file

- Organized by blocks:
 - ▶ positions
 - ▶ position errors
 - ▶ identifiers
 - ▶ ...
- Sources ordered by healpix pixel index



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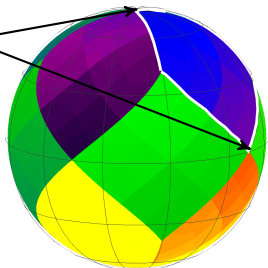
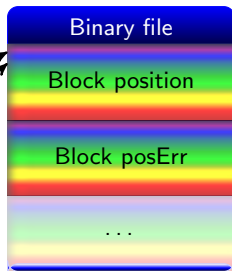
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level 0 index file		
Idx	offset	nSrcs
0	xxx	xxx
1	xxx	xxx
⋮	⋮	⋮
11	xxx	xxx



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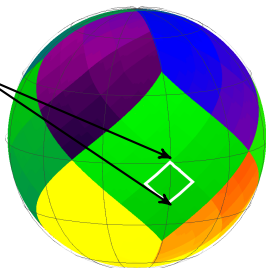
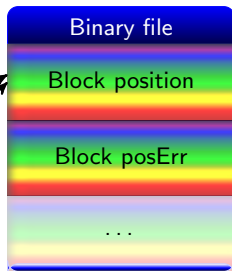
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level 2 index file		
Idx	offset	nSrcs
⋮	⋮	⋮
84	xxx	xxx
⋮	⋮	⋮



kd-tree

What is a *kd*-Tree?

- A space-partitioning data structure
- Allows for fast *k*-nearest neighbour/cone search queries
 - ▶ nearest neighbour query in $O(\log(n))$

Problem

- Naive implementation can be memory consuming
- We want a memory efficient *kd*-tree (capacity > 1 billion sources)

Solution

- To use a single array (sorted using a *kd*-tree scheme)

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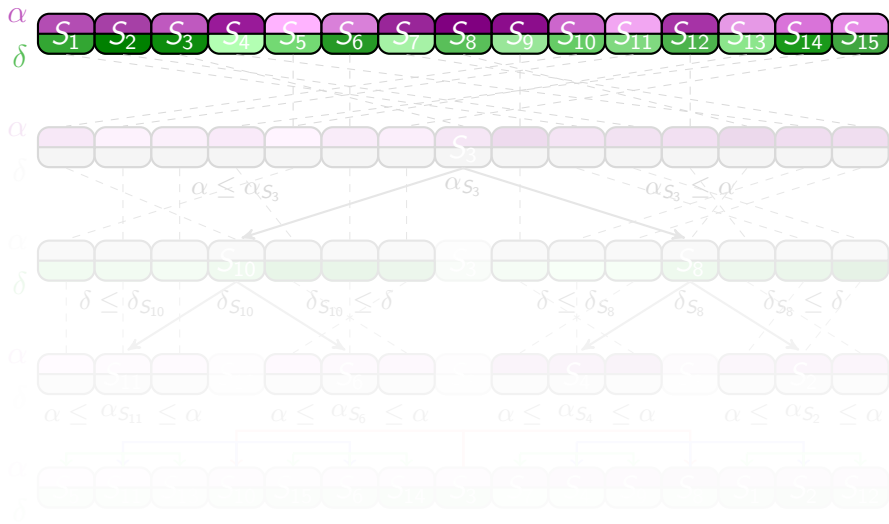
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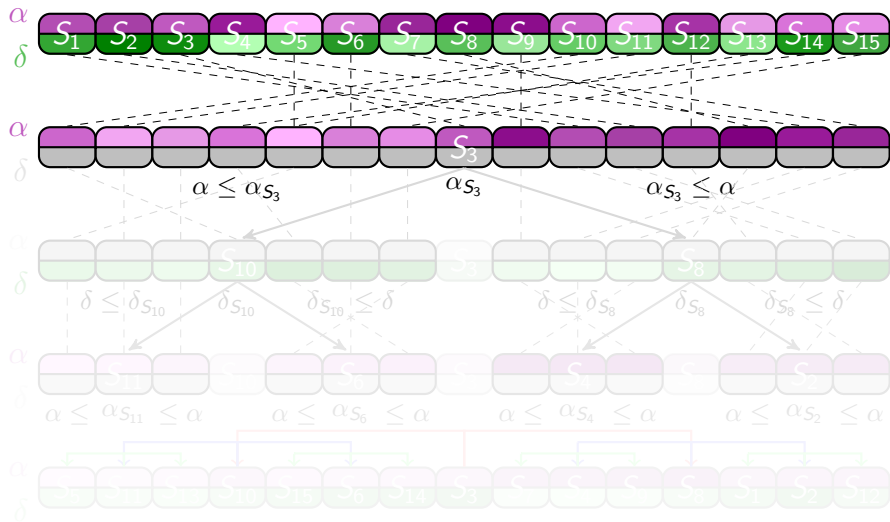
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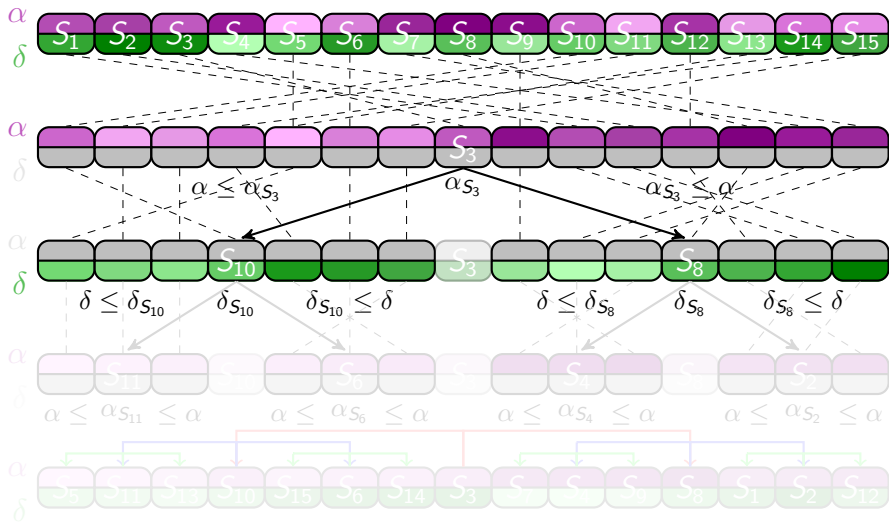
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 Algorithm: *quicksort* alternating the sorted coordinate



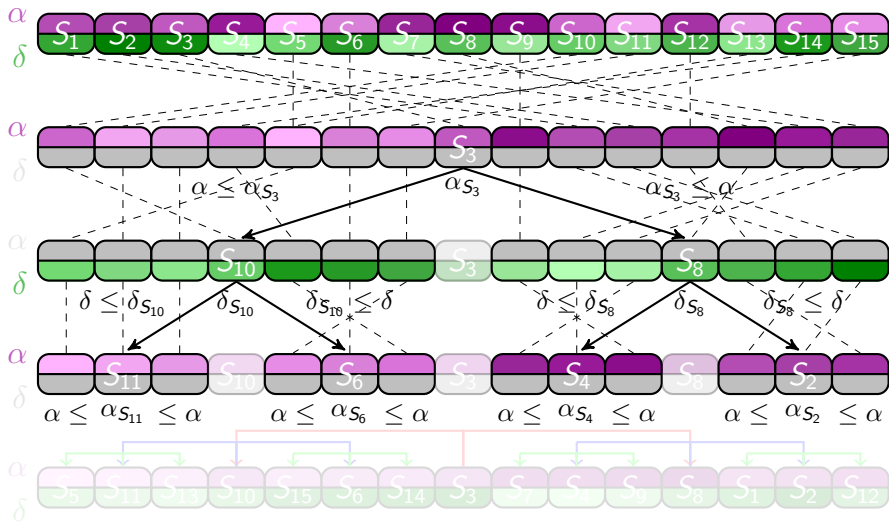
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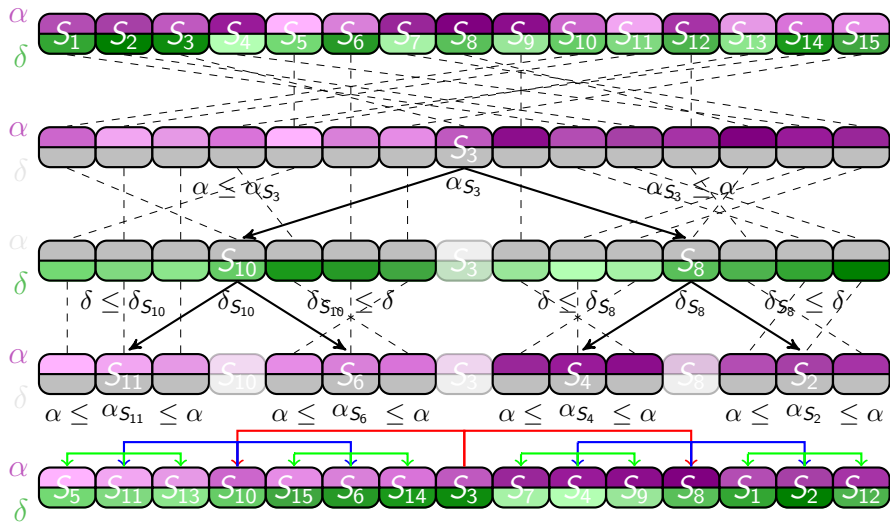


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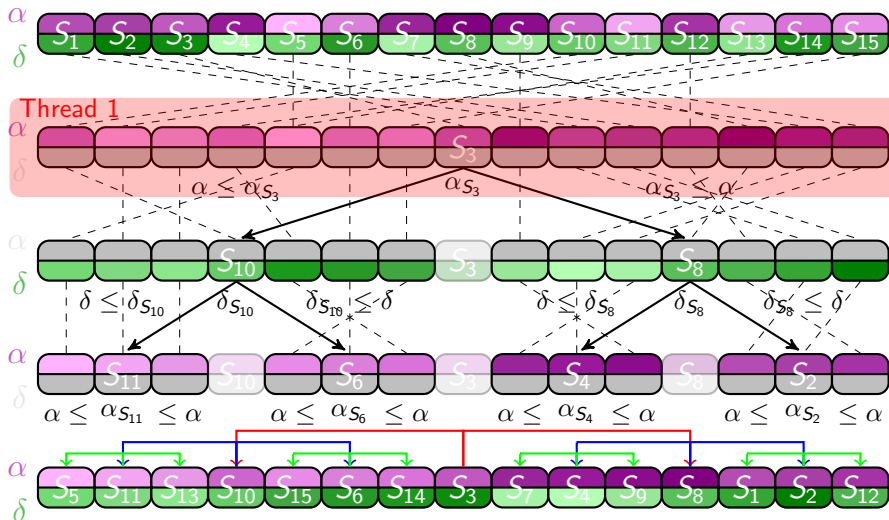
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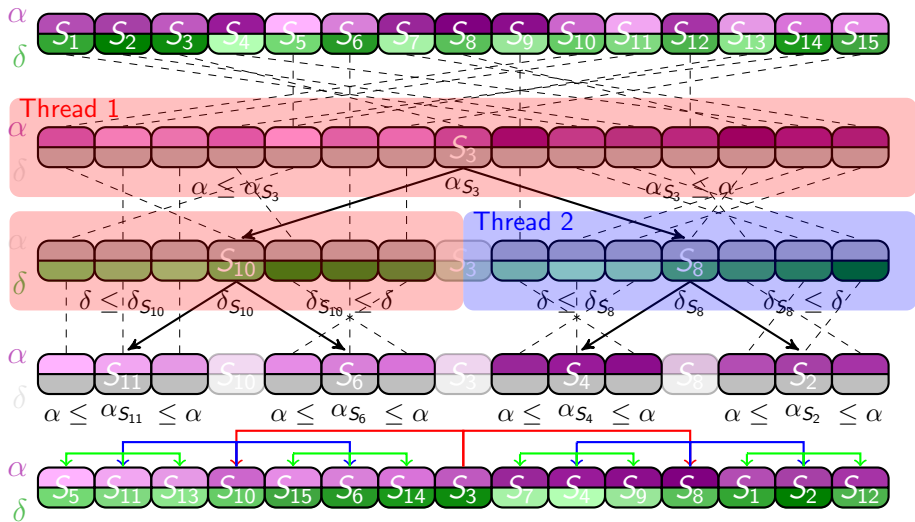
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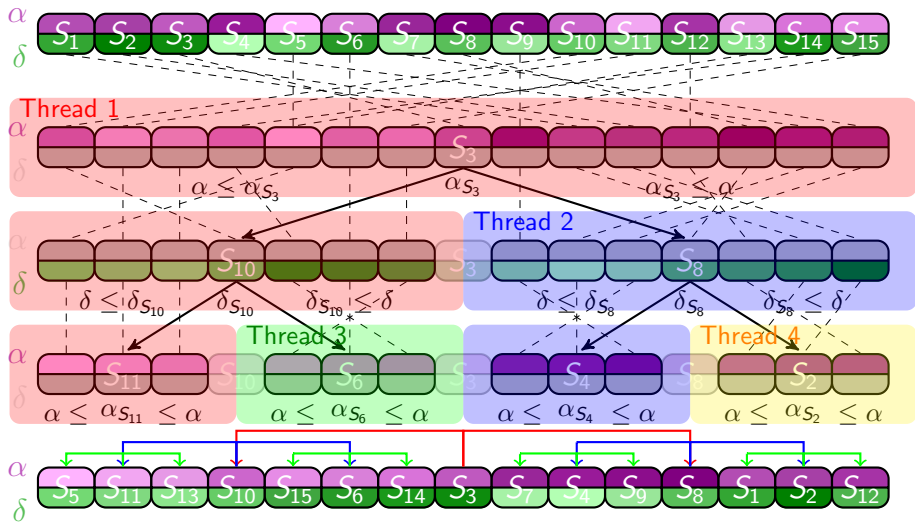
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Modified kd-tree and multithreading

Modified kd-tree

- Classical kd-tree adapted for euclidian spaces
- Solution 1: (rejected)
 - ▶ cartesian coordinates (x, y, z)
 - ★ \rightsquigarrow time consuming (conversion)
 - ★ \rightsquigarrow memory consuming (+50%)
- Solution 2: (approved)
 - ▶ spherical coordinates (α, δ)
 - ▶ classical creation algorithm
 - ▶ modified query algorithm
 - ★ angular distances (Haversine formula)
 - ★ modified circle/rectangle intersection to enter a sub-tree

Multithreading

- Single kNN or cone search query not multithread
- Pool of threads executing multiple queries simultaneously

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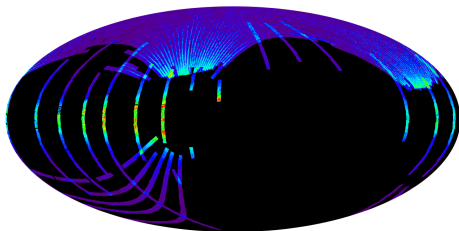
Test Machine

- Dell machine 2 600€ (~\$3 600):
 - ▶ 24 GB of **1333 MHz** memory
 - ▶ 2x Quad Core 2.27 GHz (Xeon)
 - ▶ **16 threads** (Hyper-Threading)
 - ▶ High speed HDD (10 000 rpm)

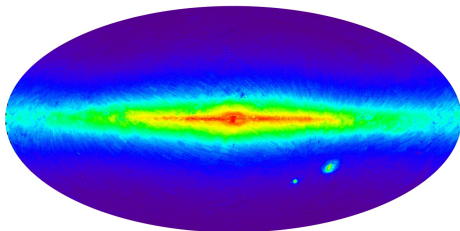


Test results

Full catalogue cross-correlation



SDSS DR7 ($\sim 357\,000\,000$ sources)



2MASS ($\sim 470\,000\,000$ sources)

- Simple cross-match: ~ 9 min

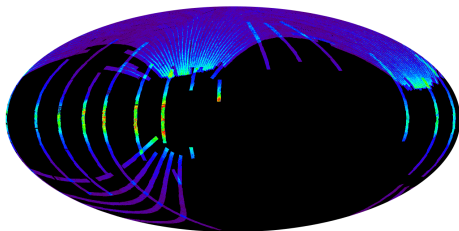
- ▶ radius of $5''$
- ▶ Healpix level 3 ($\sim 7.3^\circ$)
- ▶ Level 9 borders ($\sim 7'$)
- ▶ $\sim 49\,209\,000$ associations

- With elliptical errors: ~ 10 min

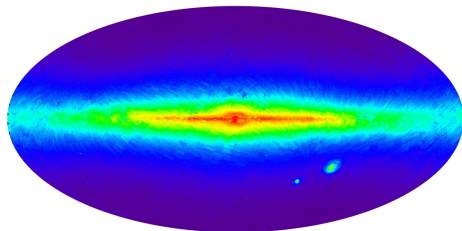
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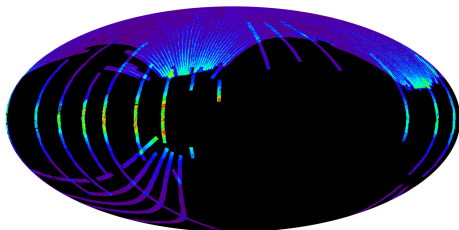
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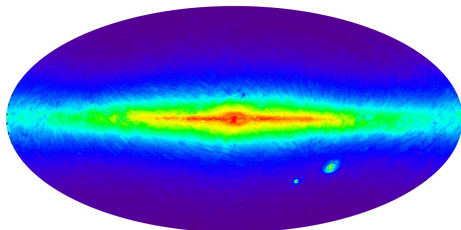
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Lessons learned

Hardware

For our application:

- RAM frequency **does** matter (lots of memory access)
- Hyper-Threading **does** matter (on 8 cores, 16 threads $\sim 2x$ faster than 8 threads)

Software: don't have *a priori*

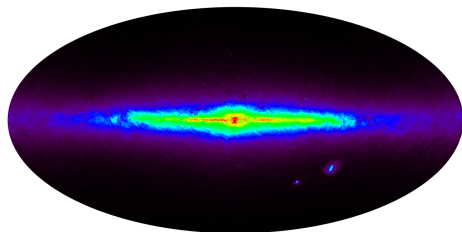
- Efficient full Java code
- Efficient modified *kd*-trees (in our case)

Service

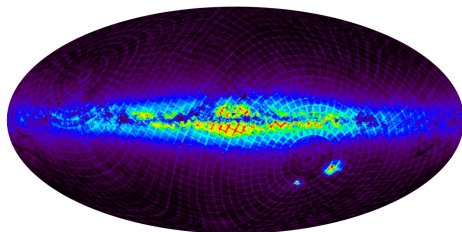
- Existing and future (very) large catalogues can be processed
- Bottleneck is data transfer (without surprise)
 - ▶ service colocated with data

Test results

Full all-sky catalogues cross-correlation



2MASS ($\sim 470\,000\,000$ sources)



USNO-B1 ($\sim 1\,046\,000\,000$ sources)

- Simple cross-match: **~ 30 min**
 - ▶ radius of $5''$
 - ▶ Healpix level 3
 - ▶ Level 9 borders
 - ▶ $\sim 583\,300\,000$ associations

Basic likelihood ratio (LR)

Ratio between:

- Rayleigh distribution

$$LR = \frac{r \exp\left(-\frac{1}{2}r^2\right)}{2\lambda r} = \frac{\exp\left(-\frac{1}{2}r^2\right)}{2\lambda}$$

- Poissonian distribution

Depends on:

- r = normalized distance in σ
- $\lambda \propto$ local density of sources

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- SDSS7 \times 2MASS correlations + LRs
- Local densities estimated by k NN averaging ($k=100$)
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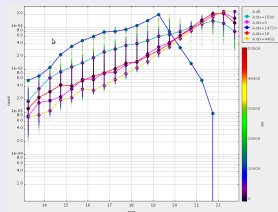
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Going further...

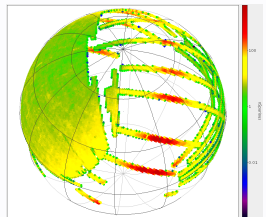
Magnitude-dependent LRs (fast solution)

- $\rho(m \pm \Delta m) = \rho p(m \pm \Delta m)$
- kNN averaging
- log N-log S law
- SDSS7, level 6 ($\sim 1^\circ$), 15 187 non empty histograms computed in 30s.



Probability of identifications (fast solution)

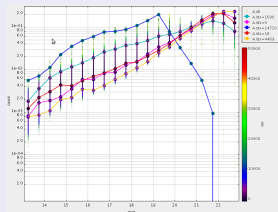
- Number of spurious match estimates
 - Positional errors sampling for both catalogues
 - $$N_{spur} = \sum_A \sum_B S_{conv} / S_{pixel}$$
- SDSS7 x 2MASS, level 6, 8min (not yet multithreaded!)



Going further...

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